

# Taipei Municipal YangMing High School

## Teacher Recruitment at 2024

### Paper and Pencil Test

Subject: Chemistry

This test consists of two parts: part I, single-choice questions (40 points); part II, short-answer questions (60 points).

Part I. Single-choice questions (1-20), 2 points for each question.

1. For  $[H^+] = (8.0 \pm 0.4) \times 10^{-5} \text{ M}$ ,  $\text{pH} = 4.10 \pm s$ .  $s = ?$   
(A) 0.01 (B) 0.02 (C) 0.03 (D) 0.04
2. What is the volume (in mL) of 1.0 M NaOH(aq) that must be added to 1.0 M, 60 mL HA(aq) to make a buffer solution with  $\text{pH} = 6.0$ ?  $\text{pK}_a = 5.7$  for HA  
(A) 20 (B) 30 (C) 40 (D) 50
3. Ionization of water is an endothermic process with  $\text{pK}_w = 14.0$  at  $25^\circ\text{C}$ . For pure water at  $37^\circ\text{C}$ , which of the following relations is correct?  
(A)  $\text{pK}_w > 14.0$  (B)  $\text{pH} = 7.0$  (C)  $\text{pOH} > 7.0$  (D)  $\text{pK}_w = 2 \text{ pH}$
4. For two monoprotic acids (HA, HB) and their conjugate bases ( $A^-$ ,  $B^-$ ), the following relations are known:  $\text{HA} + B^- \rightleftharpoons A^- + \text{HB}$ ,  $K > 1$  and  $\text{pK}_b(A^-) < 7.0$ . Which of the following order of K's is correct?  
(A)  $K_b(B^-) > K_a(\text{HB}) > K_a(\text{HA}) > K_b(A^-)$   
(B)  $K_b(A^-) > K_b(B^-) > K_a(\text{HA}) > K_a(\text{HB})$   
(C)  $K_b(B^-) > K_b(A^-) > K_a(\text{HA}) > K_a(\text{HB})$   
(D)  $K_b(B^-) > K_a(\text{HA}) > K_b(A^-) > K_a(\text{HB})$
5. The solubility of  $\text{Ag}_2\text{CrO}_4(\text{s})$  in water is 10000 times that of  $\text{Ag}_2\text{CrO}_4(\text{s})$  in 0.020 M  $\text{AgNO}_3(\text{aq})$ . What is the  $K_{sp}$  for  $\text{Ag}_2\text{CrO}_4$ ?  
(A)  $2 \times 10^{-8}$  (B)  $4 \times 10^{-10}$  (C)  $1 \times 10^{-12}$  (D)  $4 \times 10^{-12}$
6. Consider the concentration cell:  $\text{Cu} | \text{Cu}^{2+} (5.0 \times 10^{-5} \text{ M}) || \text{Cu}^{2+} (0.50 \text{ M}) | \text{Cu}$ . What is the cell potential (in volt) at  $25^\circ\text{C}$ ?  
(A) 0.06 (B) 0.12 (C) 0.18 (D) 0.24

7. For the condensation of water vapor at 1 atm and 25°C ( $\text{H}_2\text{O}(\text{g}) \rightarrow \text{H}_2\text{O}(\text{l})$ ), which of the following relations is correct?  
(A)  $\Delta G < 0$  (B)  $w < 0$  (C)  $\Delta S > 0$  (D)  $q > 0$
8. For an isothermal and reversible compression of an ideal gas, which of the following relations is correct?  
(A)  $\Delta H < 0$  (B)  $\Delta G = 0$  (C)  $q > 0$  (D)  $\Delta S < 0$
9. Adding  $\text{CH}_4(\text{g})$  into a fixed-volume flask containing  $\text{O}_2(\text{g})$  until the pressure is tripled, how many times its density will be? ( $d_{\text{final}}/d_{\text{initial}} = ?$ )  
(A) 2 (B) 3 (C) 4 (D) 6
10. Which of the following elements has the lowest second ionization energy?  
(A) B (B) C (C) N (D) O
11. For  $\text{Ag}^+$  ion in its ground state, what is the number of electrons that have  $m_l = 0$  and  $m_s = -1/2$ ? ( $Z = 47$  for Ag)  
(A) 9 (B) 10 (C) 18 (D) 20
12. Which of the following compounds would have the largest melting point?  
(A) NaCl (B) KCl (C) MgO (D)  $\text{MgCl}_2$
13. One mole of an ideal gas ( $C_v = 20 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$ ), initially at 1.0 atm and 300 K, absorbs 100 J of heat and performs 500 J of work in a certain process. What is the final temperature (in K) of the gas?  
(A) 280 (B) 290 (C) 300 (D) 320
14. Decomposition of 2.76 g  $\text{M}_2\text{CO}_3$  yields 1.88 g  $\text{M}_2\text{O}$ . What is the atomic mass of M?  
(A) 9 (B) 23 (C) 39 (D) 85
15. For a triprotic acid  $\text{H}_3\text{A}$  with  $\text{p}K_1 = 3.0$ ,  $\text{p}K_2 = 6.0$  and  $\text{p}K_3 = 9.0$ , which of the following relations is correct?  
(A)  $[\text{H}_3\text{A}] = [\text{A}^{3-}]$  at pH = 7.0  
(B)  $[\text{HA}^{2-}]/[\text{A}^{3-}] = 10$  at pH 7.0  
(C)  $[\text{H}_2\text{A}^-] > [\text{HA}^{2-}]$  at pH 6.5  
(D)  $[\text{H}_3\text{A}] > [\text{HA}^{2-}]$  at pH 5.0

16. Which of the following statements is correct?
- (A) a saturated solution contains a high concentration of solute.
  - (B) the solubility of solids always increases with temperature.
  - (C) a saturated solution involves a dynamic equilibrium between the solid and its solution.
  - (D) a supersaturated solution involves a dynamic equilibrium between the solid and its solution.
17. Which operation will increase the quantity of product for the exothermic reaction:
- $$2\text{SO}_2(\text{g}) + \text{O}_2(\text{g}) \rightleftharpoons 2\text{SO}_3(\text{g})$$
- (A) a decrease in volume of container
  - (B) an increase in temperature
  - (C) increasing P by adding some argon
  - (D) adding a catalyst
18. Consider the equilibrium:  $\text{PCl}_5(\text{g}) \rightleftharpoons \text{PCl}_3(\text{g}) + \text{Cl}_2(\text{g})$ ,  $K_c = 0.025$  at 400 K. If 0.5 mol of  $\text{PCl}_5$  is placed in a 1.0 L container at 400 K and is allowed to reach equilibrium, what is the total pressure (in atm) of the gases?
- (A) 5 (B) 10 (C) 15 (D) 20
19. For an ideal gas, which of the following sets of variables has a linear relationship?
- (A) P vs.  $1/V$  (B) V vs. T (C) PV vs. T (D) P/T vs. density
20. It took 2 min for 0.20 L of  $\text{H}_2$  to effuse through a pin hole. How long will it take (in min) for 0.10 L of  $\text{O}_2$  to effuse under identical conditions?
- (A) 2 (B) 4 (C) 8 (D) 16

Part II. Short-answer questions (21-26); 10 points for each question.

**Question 26 must be answered in English; other questions can be answered in Chinese.**

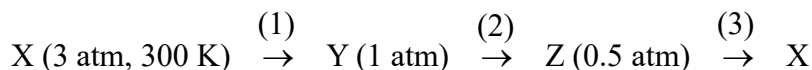
21. A certain liquid (X) has a normal boiling point of 353 K. The densities (in g/L) of the vapor X in equilibrium with its liquid at 300 K and 353 K are 0.50 and 2.7, respectively. Assume the vapor behaves ideally, answer the following questions.

- (A) Find the molar mass of X. 3%
- (B) Find the vapor pressure of liquid X at 300 K. 2%
- (C) If the saturated vapor of X at 353 K in a 2.0 L glass flask is cooled to 300 K, what is the mass of X that will be condensed? 2%
- (D) If X is a hydrocarbon containing 92.3% carbon, what are the empirical formula and molecular formula of X? 3%

22. A battery is constructed from two half cells:  $\text{Zn}|\text{Zn}^{2+}(1.0\text{ M})$  and  $\text{Mn}|\text{Mn}^{2+}(1.0\text{ M})$ ; the volume of each electrolyte solution is 300 mL. The battery is allowed to discharge at a constant current of 9.65 amperes. Given that:  $F = 96500\text{ C}\cdot\text{mol}^{-1}$ ;  $E^\circ = -0.76\text{ V}$  for  $\text{Zn}^{2+}/\text{Zn}$  and  $-1.18\text{ V}$  for  $\text{Mn}^{2+}/\text{Mn}$ . Answer the following questions.

- (A) Indicate the anode, cathode, and direction of electron flow of the cell. 3%
- (B) Calculate the standard cell potential. 2%
- (C) The equilibrium constant of the cell reaction is K;  $\log K = ?$  2%
- (D) Find  $[\text{Zn}^{2+}]$  after 10 min. of discharging. 3%

23. One mole of an ideal gas ( $C_v = 2R$ ), initially at X, undergoes three reversible steps of a cycle as shown below:

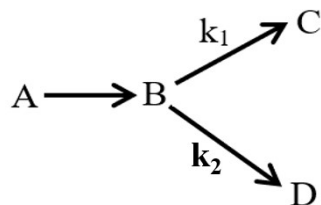


(1) isothermal; (2) isochoric (fixed V); (3) adiabatic

Answer the following questions. ( $\ln 3 = 1.1$ )

- (A) Find the temperature (T) at state Z. 2%
- (B) Find the work done (w) for step (3). 2%
- (C) Find the change in enthalpy ( $\Delta H$ ) for step (2). 3%
- (D) Find the heat (q) involved in a cycle. 3%

24. After people take the medicine X, it can be absorbed into the body through pathway  $A \rightarrow B$  and enter the blood. Medicine in the blood can reduce its concentration through decomposition ( $B \rightarrow C$ ) or excretion ( $B \rightarrow D$ ), as shown in the figure below:



Assume that the process  $A \rightarrow B$  is much faster than those of  $B \rightarrow C$  and  $B \rightarrow D$ . Therefore, each time a medicine with a dose of  $[X]_0$  is taken, it can be regarded as immediately producing a concentration of  $[X]_b (= 0.020 \text{ mM})$  of X in the blood. Assume that  $B \rightarrow C$  and  $B \rightarrow D$  are both first-order processes, and their rate constants are  $k_1 (= 0.075 \text{ h}^{-1})$  and  $k_2 (= 0.025 \text{ h}^{-1})$ , respectively. If a person takes the same dose ( $[X]_0$ ) of the medicine every  $t$  hour, answer the following questions.

- (A) Just after taking the medicine for the  $n^{\text{th}}$  time, its concentration in the blood is equal to  $[P]_n$ . Express  $[P]_n$  as a function of  $[X]_b$ ,  $k_1$ ,  $k_2$  and  $t$ . 3%
- (B) Continue to take the medicine every 6 hours for a long period of time ( $n \rightarrow \infty$ ), calculate  $[P]_\infty$  (in mM)? 3%
- (C) Find the half-life of the medicine in the blood. 2%
- (D) What proportion of the decrease in medicine concentration in the blood is caused by decomposition? 2%

25. Extraction and spectroscopic methods can be used to determine the dissociation constant ( $K_a$ ) of a monoprotic organic acid (HA) and its distribution coefficient ( $K_d$ ) between the organic phase and the aqueous phase. When extracting organic acids, it is assumed that only HA is soluble in the organic layer, and its concentration is  $[HA]_{org}$ ; while HA and  $A^-$  exist in the aqueous layer, and their concentrations are  $[HA]_{aq}$  and  $[A^-]_{aq}$ , respectively. The distribution coefficient is defined as  $K_d = [HA]_{org}/[HA]_{aq}$ .

In an extraction experiment, take 10-mL of an aqueous solution containing 3.5 mM HA at pH 5.0; extract it with 15-mL of an organic solvent. Separate the mixed solution into aqueous and organic layers. Take 1.0 mL of the aqueous layer; put it into a 1.0-cm (path length) cuvet; measure the absorbances at 400 nm and 450 nm; the observed absorbances are 0.30 and 0.62, respectively. Given the following information: molar absorptivity  $\epsilon$  (in  $M^{-1}\cdot cm^{-1}$ ):  $\epsilon_{400}(HA) = 2000$ ,  $\epsilon_{400}(A^-) = 250$ ,  $\epsilon_{450}(HA) = 200$ ,  $\epsilon_{450}(A^-) = 1500$ . Answer the following questions.

- (A) Find  $[HA]_{aq}$  and  $[A^-]_{aq}$  in the aqueous layer. 4%
- (B) Find  $[HA]_{org}$  in the organic layer. 2%
- (C) Find the acid dissociation constant  $K_a$ . 2%
- (D) Find the distribution coefficient  $K_d$ . 2%

26. Explain the following terms. 2 points for each term.

- (A) mean free path
- (B) isotonic solutions
- (C) cathodic protection
- (D) ion-selective electrode
- (E) amphoteric substance